${\bf locl\text{-}pre\text{-}preserving}^{11,40}$

f is locl-pre-preserving on $P\equiv_{\mathrm{def}} f$ is $\lambda e, e'.$ $e\leq_{\mathrm{loc}} e'$ -pre-preserving on P clarification:

 $\text{locl-pre-preserving}(\textit{es}; \textit{f}; \textit{P}) \ \equiv_{\text{def}} \ \text{rel-pre-preserving}(\textit{es}; \textit{f}; \textit{P}; \lambda \textit{e}, \textit{e}'. \ \text{es-le}(\textit{es}; \textit{e}; \textit{e}'))$